

Statically indeterminate problems

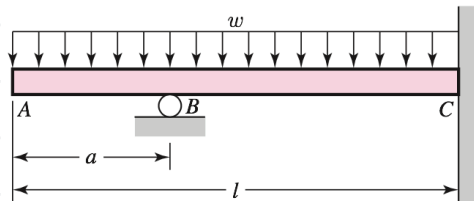
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Suppose a mechanical system has **redundant constraints** — those that constrain the system in the same manner. The forces + moments of these systems cannot be solved for with force + moment balance equations, alone. There will be an extra unknown variable for each redundant constraint.

We call such systems **statically indeterminate**. They can be solved by writing a deflection equation at the point of each redundant constraint (which gives an extra equation).

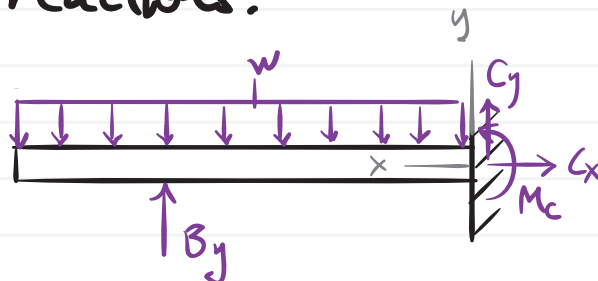
Example

For the beam shown, determine the support reactions using superposition and procedure 1 from Sec. 4-10.



1. Determine redundant reactions.

Choose B_y to be the redundant reaction.



2. Static balance equations

$$\begin{array}{l|l|l} \Sigma F_x = 0 \Rightarrow & \Sigma F_y = 0 & \Sigma M_c = 0 \\ C_x = 0 \quad (1) & B_y + C_y - wL = 0 & -B_y(L-a) + \frac{wL^2}{2} + M_c = 0 \\ & (2) & (3) \end{array}$$

3. Deflection equation.

$$\begin{aligned} \text{beam 2: } y_{B_2} &= \frac{-B_y(l-a)^2}{6EI} ((l-a) - 3(l-a)) \\ &= \frac{+B_y(l-a)^3}{3EI} \end{aligned}$$

$$\text{beam 3: } y_{B_3} = \frac{w(l-a)^2}{24EI} (4l(l-a) - (l-a)^2 - 6l^2)$$

$$\text{total: } y_{B_1} + y_{B_2} = 0 \quad (4)$$

4. Solve. Solve the simultaneous, linear system of equations (1)-(4) to find our unknown reactions B_y, C_x, C_y, M_c .