## 12.4 tf.exe Exercises for Chapter 12 tf

### Exercise 12.1 scallywag

Use a computer to solve this problem. Consider the transfer function

$$H(s) = \frac{10(s+3)}{(s+2)(s^2+8s+41)}.$$

- a. What are poles and zeros of H?
- b. Comment on the stability of the system described by H (justify your comment).
- c. Construct a pole-zero plot.
- d. Use a function like the Python control package function  $\label{eq:step_response} step\_response \ to \ simulate \ the \ unit \ step\ response \ of \ the \ system \ and plot \ it \ for \ t \in [0,3] \ seconds.$

#### Exercise 12.2 swashbuckling

Consider a system with linear state-space model matrices

$$A = \begin{bmatrix} -1 & 4 \\ 0 & -3 \end{bmatrix} \qquad B = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$C = \begin{bmatrix} 1 & 0 \end{bmatrix} \qquad \qquad D = \begin{bmatrix} 0 \end{bmatrix}. \tag{1b}$$

- 1. Derive the transfer function H(s) for the system. Express it as a single ratio in s.
- 2. What are the poles and zeros?
- 3. Compare the poles to the eigenvalues of A.
- 4. Draw or sketch a pole-zero plot.
- 5. With reference to the pole-zero plot, comment on the stability and transient free response characteristics of the system.
- 6. Use the inverse Laplace transform  $\mathcal{L}^{-1}$  to find the system's forced response y(t) to step input  $u(t) = 9 u_s(t)$ .

#### Exercise 12.3 boris

Consider a mass-spring-damper system with mass m, spring constant k, and damping coefficient B with the I/O ODE

$$\ddot{y} + \frac{B}{m}\dot{y} + \frac{k}{m}y = \frac{1}{m}u$$

for input force  $u(t) = F_S(t)$  and output position  $y(t) = x_m(t)$ .

- a. Find the corresponding transfer function H(s) = Y(s)/U(s).
- b. Find the natural frequency and damping ratio in terms of system parameters m, k, and B.
- c. What are poles and zeros of H in terms of system parameters m, k, and B?
- d. For system parameters m = 10 kg,  $k = 1 \cdot 10^5$  N/m, and B = 500 N·s/m, construct a pole-zero plot.
- e. Comment on the stability of the system described by H. Are there any values of system parameters m, k, and B for which the system is marginally stable or unstable?
- f. For system parameters m=10 kg,  $k=1\cdot 10^5$  N/m, and B=500 N·s/m, use a function like the Python control package function step\_response() to simulate the unit step response of the system and plot it for  $t\in [0,0.3]$  s.

# 13 imp