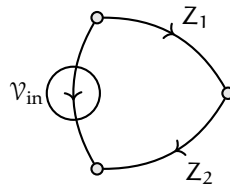


## 13.6 imp.divide The divider method



**Figure divide.1:** the two-element cross-variable divider.

**1** In *Electronics*, we developed the useful voltage divider formula for quickly analyzing how voltage divides among series electronic impedances. This can be considered a special case of a more general **across-variable divider** equation for any elements described by an impedance. After developing the across-variable divider, we also introduce the through-variable divider, which divides an input through-variable among parallel elements.

### Across-variable dividers

**2** First, we develop the solution for the two-element across-variable divider shown in [Figure divide.1](#). We choose the across-variable across  $Z_2$  as the output. The analysis follows the impedance method of [Lecture 13.3 imp.tf](#), solving for  $v_2$ .

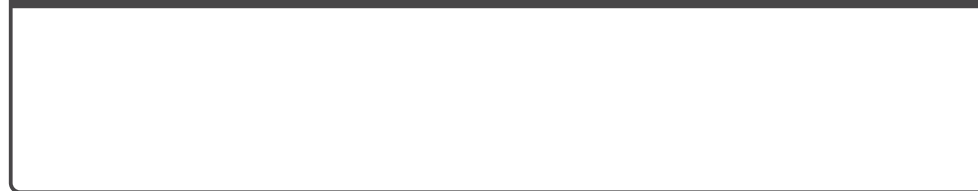
1. Derive four independent equations.
  - a) The normal tree is chosen to consist of  $v_{in}$  and  $Z_2$ .
  - b) The elemental equations are

- c) The continuity equation is
- d) The compatibility equation is

2. Solve for the output  $v_2$ . From the elemental equation for  $Z_2$ ,



- 3 A similar analysis can be conducted for  $n$  impedance elements.

**Equation 1 general across-variable divider****Through-variable dividers**

- 4 By a similar process, we can analyze a network that divides a through-variable into  $n$  *parallel* impedance elements.

**Equation 2 general through-variable divider****Transfer functions using dividers**

- 5 An excellent shortcut to deriving a transfer function is to use the across- and through-variable divider rules instead of solving the system of algebraic equations, as in [Lec. 13.3 imp.tf](#). An algorithm for this process is as follows.

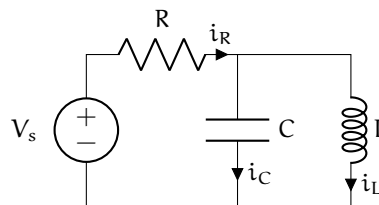
1. Identify the element associated with an output variable  $Y_i$ . Call it the *output element*.
2. Identify the source associated with an input variable  $U_j$ . Set all other sources to zero.
3. Transform the network to be an across- or through-variable divider that includes the “bare” (uncombined) output element’s output variable.<sup>6</sup>
  - a) If necessary, form equivalent impedances of portions of the network, being sure to leave the output element’s output variable alone.
  - b) If necessary, transform the source *à la* Norton or Thévenin.
4. Apply the across- or through-variable divider equation.
5. If necessary, use the elemental equation of the output element to trade output across- and through-variables.
6. If necessary, use the source transformation equation of the input to trade input across- and through-variables.
7. Divide both sides by the input variable.

**6** It turns out that, despite its many “if necessary” clauses, very often this “shortcut” is easier than the method of [Lecture 13.3 imp.tf](#) for low-order systems if only a few transfer functions are of interest.

### Example 13.6 imp.divide-1

Given the circuit shown with voltage source  $V_s$  and output  $v_L$ ,

- a. what is the transfer function  $\frac{V_L}{V_s}$ ?
- b. Without transforming the source, find the transfer function  $\frac{I_L}{V_s}$ .
- c. Transforming the source, find  $\frac{I_L}{V_s}$ .



re: a  
circuit  
transfer  
function  
using  
a  
divider

<sup>6</sup>In other words, if the across-variable of the output element is the output, do not combine it in series; if the through-variable is the output, do not combine it in parallel.

