

14.3 nlin.exe Exercises for Chapter 14 nlin

Exercise 14.1 sigmund

Consider a nonlinear capacitor with constitutive equation relating charge q_C and voltage v_C :

$$q_C = kv_C^{3/2} \quad (1)$$

with k a positive constant.

- Derive an elemental equation relating dv_C/dt and i_C for the nonlinear capacitor.
- From the elemental equation, what is the voltage-dependent capacitance $C(v_C)$?
- Consider the RLC-circuit of Fig. exe.1, which includes the nonlinear capacitor. Derive a nonlinear state-space equation with state vector

$$\mathbf{x} = [v_C \quad i_L]^T. \quad (2)$$

- For a constant input $V_S(t) = 5 \text{ V}$, derive the equilibrium state.
- Linearize the state-space equation about the operating point

$$\mathbf{x}_o, \mathbf{u}_o = [5 \text{ V} \quad 0 \text{ A}]^T, [5 \text{ V}]. \quad (3)$$

Define the state equation matrices A and B , the linearized state and input vectors \mathbf{x}^* and \mathbf{u}^* , and the linearized state equation.

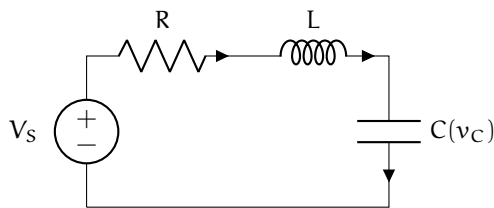


Figure exe.1: circuit for Exercise 14.1 nlin..

Exercise 14.2 franz

A nonlinear diode model gives a diode's elemental equation to be

$$i_D = I_s(\exp(v_D/V_{TH}) - 1).$$

We let the saturation current be $I_s = 10^{-12}$ A and the thermal voltage be $V_{TH} = 0.025$ V. Considering this nonlinear diode model for the circuit of Fig. exe.2.

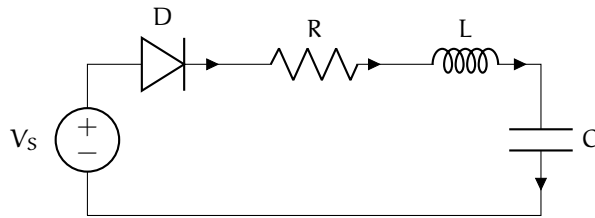


Figure exe.2: circuit for Exercise 14.2 nlin..

- a. Derive a nonlinear state-space equation with state vector

$$\mathbf{x} = [v_C \quad i_L]^T. \quad (4)$$

Hint: include the diode in your normal tree.

- b. For a constant input $V_s(t) = 0$ V, derive the equilibrium state.
 c. Linearize the state-space equation about the operating point

$$\mathbf{x}_o, \mathbf{u}_o = [0\text{V} \quad 0\text{A}]^T, [0\text{V}]. \quad (5)$$

Hint: $d \ln(x)/dx = 1/x$. Define the state equation matrices A and B, the linearized state and input vectors \mathbf{x}^ and \mathbf{u}^* , and the linearized state equation.*

15 phase

16 sim
