

01.3 algtri.matrix Matrix inverses

This is a guide to inverting 1×1 , 2×2 , and $n \times n$ matrices.

Let A be the 1×1 matrix

$$A = [a].$$

The inverse is simply the reciprocal:

$$A^{-1} = [1/a].$$

Let B be the 2×2 matrix

$$B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix}.$$

It can be shown that the inverse follows a simple pattern:

$$\begin{aligned} B^{-1} &= \frac{1}{\det B} \begin{bmatrix} b_{22} & -b_{12} \\ -b_{21} & b_{11} \end{bmatrix} \\ &= \frac{1}{b_{11}b_{22} - b_{12}b_{21}} \begin{bmatrix} b_{22} & -b_{12} \\ -b_{21} & b_{11} \end{bmatrix}. \end{aligned}$$

Let C be an $n \times n$ matrix. It can be shown that its inverse is

$$C^{-1} = \frac{1}{\det C} \text{adj } C,$$

where adj is the **adjoint** of C .

Bibliography

- Agarwal, A. **and** J. Lang (2005). *Foundations of Analog and Digital Electronic Circuits*. The Morgan Kaufmann Series in Computer Architecture and Design. Elsevier Science. ISBN: 9780080506814.
- Horowitz, P **and** W Hill (2015). *The Art of Electronics*. Cambridge University Press. ISBN: 9780521809269.
- Ulaby, Fawwaz T., Michel M. Maharbiz **and** Cynthia M. Furse (2018). *Circuit Analysis and Design*. ISBN 978-1-60785-484-5. Michigan Publishing.